DESIGN OF ARTIFICIAL NEURAL NETWORKS

USING EVOLUTIONARY COMPUTATION

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2. Genetic algorithms

3. Designing ANN with evolutionary computation

- 3.1. Connection weights in a defined architecture
- 3.2. Evolution of architectures
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INTRODUCTION-I

- ANNs are a biologically-inspired attractive paradigm of computation for many applications: pattern recognition, system identification, cognitive modeling, etc.
- Properties of ANNs are:

Capability of "learning" and "self-organizing" to carry out a given task: ill-defined and input/output mapping.

- Potential for massively parallel computation.
- Robustness in the presence of noise.

Resilience to the failure of components.

 Practical applications require the choice of a suitable network topology, the learning rule and the processing function computed by individual units



INTRODUCTION-II

- ANNs are often hard to design because:
 - ➡ Many basic principles governing information processing are difficult to understand.
 - Complex interactions among networks unit make engineering techniques inapplicable.
 - The scaling problem: some solutions are not good if the complexity of the problem increases.

• In addition to experience and trial and error methods to design an ANN, how could we appeal to more efficient automated procedures? Using EVOLUTIONARY COMPUTATION.

 Genetic Algorithms, Evolution Strategies and Evolutionary Programming: population-based stochastic search algorithms, inspired in principles of natural evolution



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GENETIC ALGORITHMS-I

• GAs are based on the Darwin's evolution and natural selection concepts.

• GAs are systematic methods to resolve searching and optimization problems, applying analog methods than the biological evolution: selection based on population, reproduction and mutation.

• An optimization problem consist of:

- Space of search Σ with M symbols and dimension M^N. Any point in this space is a vector of N components of the M symbols.

- A fitness or cost function F: $\Sigma \rightarrow \mathbf{R}$, to be optimized.

- General framework of a GA.
- 1. Generate the initial population P(0) at random, and set i=0;

2. REPEAT

- a) Evaluate each individual in the population;
- b) Select parents from P(i) base on their fitness in P(i);
- c) Applied search operators to parents and produce offspring which form P(i+1);

d) i=i+1;

3. UNTIL termination criterion is satisfied.



GENETIC ALGORITHMS-II

• The individuals of the population are chromosomes or genotypes: arbitrary data structure that encodes a certain solution to the problem. Its meaning, in relation with the problem at hand, is a phenotype. Different genotypes may encodes for the same solution or phenotypes, but the reverse does not hold.

 Each component of the chromosome represents a gene, and the molecular base of the gene is the ADN.

• The gene is said to be in several states, called alleles (feature values), and its position in the string, loci (string positions):

 $A = a_1 a_2 a_3 a_4 a_5 a_6 a_7$ A= 0 1 1 1 0 0 0





GENETIC ALGORITHMS-III

Advantages:

- It is enough with a small, and even null, knowledge a priori of the characteristics of the problem to be solved.
- It is not necessary the direct control of the environment.
- Neither is necessary to search in the whole space of possible solutions.
- They use global information
- The characteristics acquired by the parents during the evolution are inherited by the offspring.
- Robustness. GAs are capable of finding a good solution

Limitations:

- The epistasis problem: iterations not wanted among the genes, in which a gene suppresses the expression of another. To solve it, elitist selection.
- Premature convergence. Selection to get o good trade-off between exploration and exploitation.
- Long computation times. Parallelization of the algorithm or distribute the population

• Fall in local minima



Evaluation and selection:

Evaluation is performed through the fitness function.

Selection probability

$$p_s(i) = \frac{f(i)}{\sum_{i=1}^{N} f(i)}$$

Fitness proportionate selection with the roulette wheel method

Nº	CADENA	FITNESS	% DEL TOTAL	
1	01101	169	14,4	
2	11000	576	49,2	
3	01000	64	5,5	
4	10011	361	30,9	
TOTAL		1170	100,0	



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➡ Mutation operator: it simulate transcription error that can happen with very low probability, p_m, when a chromosome is duplicated.

Mutation contributes with new information, essential for the evolution, that is, it introduces diversity in the population.



The performance of a GA depends on: dimension of the population, application frequency of the selection, crossover and mutation operators, and how these operators are used.
Optimization of a polynomial function:

- . Binary encoding
- . Population= 100 individuals
- . Length of each individual = 30
- . Study interval:[0,230]
- $p_{c} = 0.5$
- $p_{\rm m} = 0.03$

After 7 generations, the average fitness has been stabilized.



Optimization of a polynomial function:

- . Binary encoding
- . Population= 10 individuals
- . Length of each individual = 10
- . Study interval:[0,2¹⁰]
- $p_{c} = 0.5$
- . p_m = 0.03

Small population and short length of individuals makes the effect of mutation operator very active and the GA does not work properly.



EXAMPLE: Optimization of a polynomial function: . Binary encoding . Population= 10 individuals . Length of each individual = 10. Study interval: [0,2¹⁰] PROMEDIO $p_{c} = 0.3$ **FITNESS** $p_{\rm m} = 0.03$ 0.957 0.686 The GA behaves incorrectly due to low $p_c = 0.3$. 0.415 50 26 1 **GENERACIONES** Dpto. Tecnología Electrónica Universidad de Málaga

THE SCHEMA THEOREM

 $rac{}$ Binary alphabet $\Omega = \{0,1\}$; extended alphabet $\Omega' = \{0,1,*\}$

A schema E represents all strings, which match it on all positions other than *. The schema (*101) matches two strings: {(0101),(1101)}

 \Rightarrow Number of possible schematas=(base+metasymbol)^m, with *m* the length of an individual.

 \Rightarrow Every schema E matches 2^r strings, with *r* de number of metasymbols. The schema (*1*0) matches four strings

Sech string of the length m is matched by 2^m schemata.

r Order O(E)= Number of fixed positions in the template string. O(10**11)=4; O(1****)=1

➡ Length L(E)= Distance between the first and last fixed positions in its template string. It is a measure of compactness information.

L(10**11)=6-1=5; L(1*****)=1-1=0

 \Rightarrow Fitness at time t, F(E,t)= Average fitness of all strings in the population matched by the schema E.



MEANING OF OPERATORS

 $S(E,t+1) = S(E,t) \cdot \frac{f(E)}{E}$

Selection:

Crossover:
$$p_s = 1 - p_d = 1 - \frac{p_c \cdot L(E)}{m - 1}$$
 $p_s \ge 1 - \frac{p_c \cdot L(E)}{m - 1}$

Mutation: $p_s = (1 - p_m)^{O(E)}; p_m \ll 1 \Rightarrow p_s \approx 1 - O(E) \cdot p_m$

Combined effects:

$$S(E,t+1) \ge S(E,t) \cdot \frac{f(E)}{\bar{f}} (1 - \frac{p_c \cdot L(E)}{m-1} - O(E) \cdot p_m)$$

Building Block hypothesis: A genetic algorithm seeks near optimal performance through the juxtaposition of short, low-order, high performance schemata.



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To find the suitable weights to perform the task at hand.
Classical learning algorithms (backpropagation, conjugate gradient, ...) get trapped in local minimun and never find it if the error function is multimodal and/or non-differenciable.

➡ We may formulate the training process as the evolution of the connecting weights for a determined architecture and learning task.

Two steps: weights representation and evolutionary process.

1) Decode each individual into a set of connection weights and construct a corresponding ANN with the weights.

2) Evaluate each ANN by computing its total mean square error between actual and expected outputs. The fitness is determined by the error.

3) Select parents for reproduction based on their fitness.

4) Apply search operators to generate offspring.





Binary representation:

➡ The chromosome representing the net is a list of weights in a predefined order, each weight represented by a binary string to be decoded into real values between, for instant, -1 and +1.

It facilitates the hardware implementation of ANNs

In binary representation several encoding methods can be used: Gray, BCD, exponential, etc.

Drawbacks: poor scalability, i.e., if the number of connections increases, the length of the string increases severely, degrading the features of the GA.

➡ If higher precision is needed in the weight value, more bits have to be added to the binary representation



Real number representation:

Each chromosome is a real vector, being each component a weight.

Search space becomes very large.

It has many advantages, but requires specialized genetic operators.

Evolutionary Programming and Evolution Strategies are techniques well-suited in this kind of representation.



Permutation problem:

Networks topologically equivalent but different encoding. Any permutation of the hidden nodes produce equivalent network functions and fitness measurements.

Limit the crossover standard operator. Evolutionary programming does not use crossover



Flow diagram for designing connection weights:



Hybrid training:

- GAs are not efficient in fine-tuned local search, although they are good at global search.
- Finding initial weights with GAs and then local search with backpropagation.



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Selection of architecture is a very important task: connectivity and transfer function of each node:

- \bullet Few connections and linear nodes \rightarrow limited capability
- Many connections and non-linear nodes \rightarrow overfit noise in the training data and poor generalization.
- Usually, architecture design is performed in an unsystematic manner by guesswork and trial and error.
- Methods such as constructive-destructive algorithms are susceptible to becoming trapped at local minima and depends on the initial topology.
- Design the architecture of an ANN is a search problem in the architecture space where each point represents an architecture.
 So GAs are a promising technique.



➡ Why GAs are good candidates:

- The surface of search is infinitely large: number of possible nodes and connections is unbounded.
- The surface is non-differentiable: changes in the number of nodes or connections are discrete and can have a discontinuous effect on GAs performance.
- The surface is complex and noisy: mapping from an architecture to its performance is indirect, epistatic and dependant on the evolution method.
- The surface is deceptive: similar architectures may have quite different performance.
- The surface is multimodal: different architectures may have similar performance.





Direct encoding: all aspects of a network architecture (connections and nodes) are encoded into the chromosome.

The X-OR problem of two bits: connectivity or adjacency matrix



Matrix lower triangular: feedforward Matrix triangular: feedback

Direct encoding: relationships between genotypes and phenotype



- Drawbacks:scaling problem. Very long chromosomes
- The permutation problem
- Useful for small architectures

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Indirect encoding: only the most important parameters of an architecture are encoded (hidden layers and hidden nodes in each layer). The details of each connection is either predefined or specified by deterministic developmental rules.

Last tendency in indirect encoding is to use grammatical encoding: technique for developing or growing ANN, rather than looking for a complete network description at the individual level.

Grammatical encoding presents better scalability, reduces the effect of the permutation problem, and allows to find building blocks of general utility and of reusing developmental rules for general classes of problems.



- Developmental rule:
- Grammar: one or more productions
- Production: rewriting rule that associates a left-hand side (head) to a right-hand side (body). The two side are separated by the metasymbol →.
- Terminal elements: either 1 (connection) or 0 (nonconnection)
- The connectivity pattern of the architecture in the form of a matrix is constructed from a basis, i.e., a single element matrix, by repetitively applying suitable developmental rules to non-terminal elements till the matrix contains only terminal elements.





$$\Rightarrow \text{ Developmental rule:} S \to \begin{pmatrix} A & B \\ C & D \end{pmatrix}$$

S is the initial element
$$A \to \begin{pmatrix} a & a \\ a & a \end{pmatrix} \quad B \to \begin{pmatrix} i & i \\ i & a \end{pmatrix} \quad C \to \begin{pmatrix} i & a \\ a & c \end{pmatrix} \quad D \to \begin{pmatrix} a & e \\ a & e \end{pmatrix}$$

$$a \to \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix} \quad c \to \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} \quad e \to \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix} \quad i \to \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$$

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Development of an architecture from the initial element.



➡ Developmental rule:

$$\begin{split} S &\longrightarrow \begin{pmatrix} A & B \\ C & D \end{pmatrix} \\ A &\longrightarrow \begin{pmatrix} a & a \\ a & a \end{pmatrix} \quad B &\longrightarrow \begin{pmatrix} i & i \\ i & a \end{pmatrix} \quad C &\longrightarrow \begin{pmatrix} i & a \\ a & c \end{pmatrix} \quad D &\longrightarrow \begin{pmatrix} a & e \\ a & e \end{pmatrix} \quad \cdots \\ a &\longrightarrow \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix} \quad c &\longrightarrow \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} \quad e &\longrightarrow \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix} \quad i &\longrightarrow \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \quad \cdots \end{split}$$

Chromosome encoding



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There are some controversial with this approach

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NODE TRANSFER FUNCTIONS

➡ The transfer node in the architecture is supposed to be fixed by human expert, and often the same for all the nodes, at least for all the nodes in the same layer.

But node transfer function may evolve with GAs. Different approaches:

• For each individual in the initial population, 80% nodes use sigmoid transfer function and 20% Gaussian transfer function. The evolution was used to decide the optimal mixture between these two transfer function. The transfer function themselves were not evolvable.

• With sigmoid and Gaussian transfer nodes, the total number is not fixed, and is allowed growth and shrinking of the ANN by adding or deleting nodes.

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Usually connection weights have to be learned after a near optimal architecture is found. Evolution of architectures without connections weights brings a mayor problem: noisy fitness evaluation.

Phenotype's (an ANN with a full set of weights) fitness is used to approximate its genotype's (an ANN without any information on weights) fitness. Two mayor sources of noise:

- Different random initialization of weights may produce different training results: the same genotype could have different fitness.
- Different training algorithms may produce different training results even from the same set of initial weights.



- Evolve architecture and weights simultaneously.
- Each individual with two chromosomes: one for the area of connectivity definition (ACD) and other for the area of weight definition (AWD).



Area of weight definition:



⇒ Encoding example of an ANN with I=4, O=2, L=2, H1=3, H2=2, μ =0 and W=3.



Flow diagram for simultaneous design of architecture and weights.



➡ The N-bit parity combinatorial problem. N=3.



 μ =0 Fitness= θ(E)+ς(H)+η(W) θ(E)=λΣ_KΣj(Yj(K)-dj(K))² λ=45; ρ=30; δ=15



Sequence detection: 110



Input 1011011101011101101... Output 000010001000010010..

μ=1 λ=10⁴; ρ=10³; δ=1





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Other proposal uses Evolutionary Programming to avoid crossover operators which may destroy both ANNs to be exchanged.



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EVOLUTION OF LEARNING RULES

Training algorithm may have different performance when applied to different ANN architectures: relationship between network architecture and learning process is generally unknown.

An ANN should adjust
its learning rule adaptively
according to its
architecture and the task
to be performed.
GAs may guide the
learning rule: evolution
cycle of learning rules ⇒



EVOLUTION OF LEARNING RULES

Encoded learning is very noisy: we use Phenotype's fitness (an ANN training result) to approximate genotype's fitness (a learning rule's fitness).
The evolution of learning rules has to work on the dynamic behavior of an ANN. How to encode the dynamic behavior of a learning rule into a static chromosome? Universal representation is impractical.

Constrains:

• Weight-updating depends only of local information (activation of the input and output nodes, the current weight, ...).

•The learning rule is the same for all connections in an ANN.

A learning rule is assumed to be a linear combination of these local variables and their products:

$$\Delta w(t) = \sum_{k=1}^{n} \sum_{i_1, i_2, \cdots, i_k=1}^{n} \left(\theta_{i_1 i_2 \cdots i_k} \prod_{j=1}^{k} x_{i_j}(t-1) \right)$$

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t is time, $\Delta \omega$ is the weight change, **x**_i are local variables, and θ 's are real coefficients determined by the evolution.

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INPUT DATA SELECTION

In real problems, the possible inputs to an ANN can be quite large, and there may be some redundancy among different inputs.

Besides statistical methods, GAs can be applied to find a nearoptimal set of input features to an ANN.

➡ In the encoding of the problem, each individual in the population represents a portion of the input data.

The evolution of an individual is carried out by training an ANN with these inputs and using the result to calculate its fitness value. The ANN architecture is often fixed.



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APPLICATION TO ELECTRIC LOAD FORECASTING

➡ Power consumption in the province of Malaga during 1992-1993





APPLICATION TO ELECTRIC LOAD FORECASTING

➡ Forecasting has been performed with statistical techniques, with ANNs and with genetic ANNs.



APPLICATION TO ELECTRIC LOAD FORECASTING

Results

ER92= Training relative error for year 1992.

ER93= Forecasting relative error for year 1993.

	ER92%	ER93%	TOPOLOGÍA
ELMAN	3,6191	2,8758	8-OCULTAS
ARIMAX	3,6081	2,8815	
GÉNETICA FEED-BACK	3,6724	2,8986	5-OCULTAS 48-PESOS
ARMAX	3,6520	2,9071	
LEVENBERG MARQUARDT	3,4077	2,9354	8-OCULTAS
GENÉTICA FORWARD	3,4106	2,9360	5-OCULTAS 34-PESOS
HTA-GLOBAL	3,3718	2,9412	8-OCULTAS
RBR	4,0352	2,9595	8-OCULTAS
ARX	3,7456	2,9718	
HTA-LOCAL	3,3016	2,9728	8-OCULTAS
CC	3,3214	2,9776	6-CASCADA
OBS	3,3498	2,9815	6-OCULTAS 37-PESOS
OBD	3,3818	2,9979	7-OCULTAS 46-PESOS



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CONCLUSIONS

GAs have proved to be a powerful search method. Parallelization techniques are necessary to reduce the computation time.

GAs can be introduced into the design of ANNs at many different levels:

- The evolution of connection weights.
- To find a near-optimal architecture automatically.
- Simultaneous evolution of weights and architecture to get better results.
- To allow an ANN to adapt its learning rule to its environment

Its applicability to actual problems: electric load forecasting.

